

# Explaining the Explainers in Graph Neural Networks: a Comparative Study

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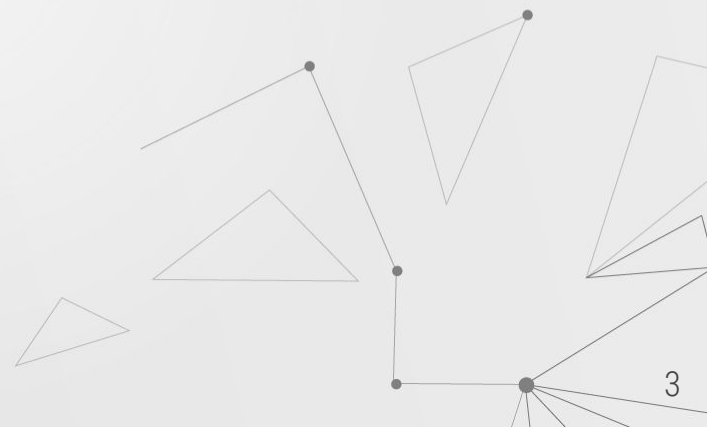
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# 01 Explainability

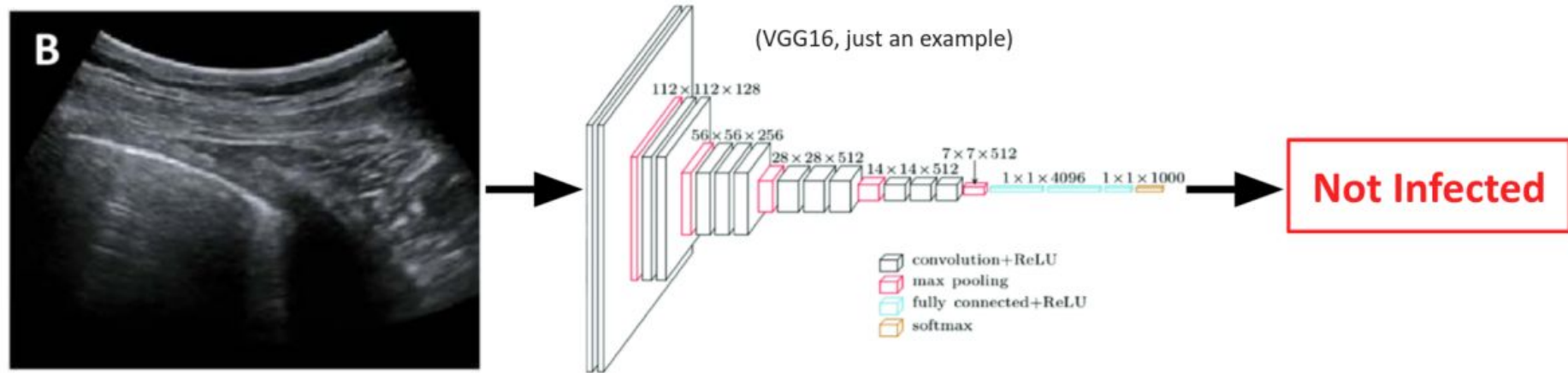
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You need to be checked for COVID-19. The doctor takes a scan of your lungs and uses a state-of-the-art deep neural network to automatically compute a diagnosis. The model thinks that you are not infected.



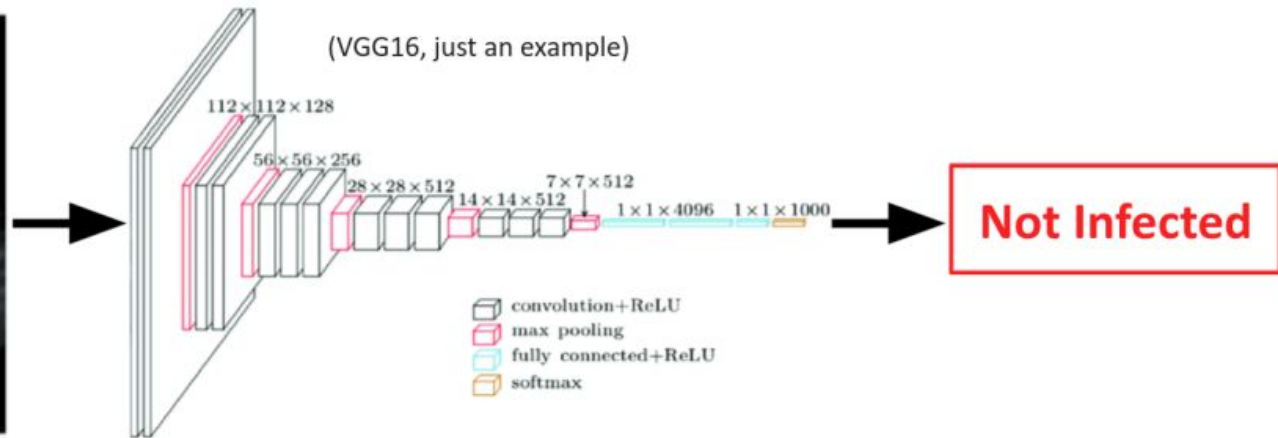
# 01 Explainability

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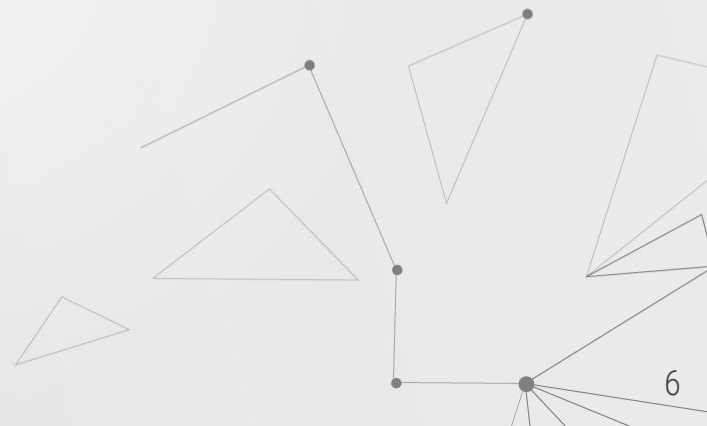
**Question:** Would you trust the model's prediction?



# 01 Explainability

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People are finding more and more ways of integrating machine learning models into applications.



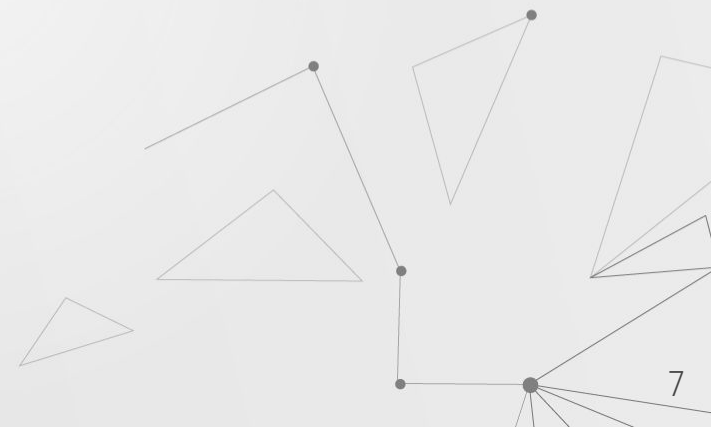


# 01 Explainability

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People are finding more and more ways of integrating machine learning models into applications.

- Medical Diagnosis
- Crime (e.g., predicting recidivism in convicts)
- Credit Scoring (e.g., approving loan requests)
- Surveillance (e.g., face recognition, profiling)
- Hiring (e.g., ranking/filtering candidates)
- ...





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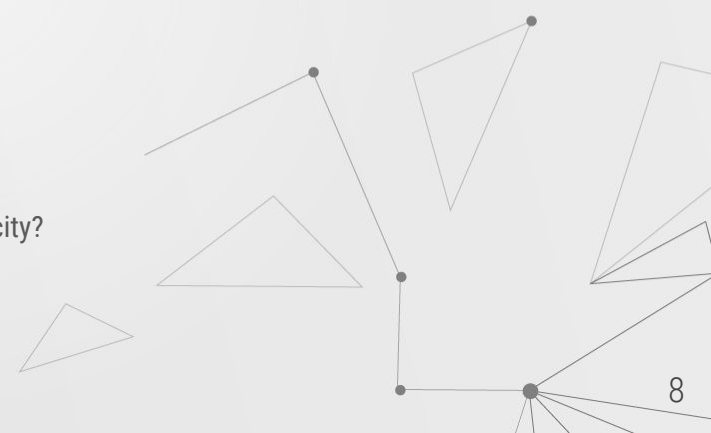
## Right of explanation:

Example: you apply for a 50,000 euro loan.

Unfortunately, your bank rejects your application.

You have a right to know why it was rejected: was it your credit history or your age/gender/ethnicity?

See [https://en.wikipedia.org/wiki/Right\\_to\\_explanation](https://en.wikipedia.org/wiki/Right_to_explanation)





# 01 Explainability

Horse-picture from Pascal VOC data set



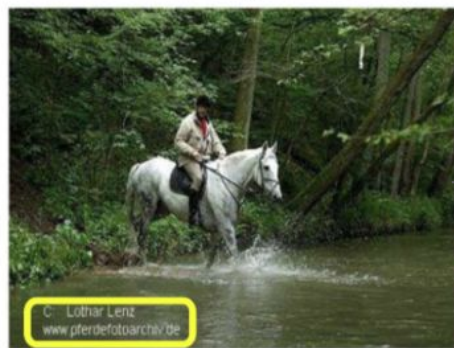
CNN

Horse class

Credit [Lapuschkin et al., 2019]

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Horse-picture from Pascal VOC data set



**CNN**

Horse class



**CNN**

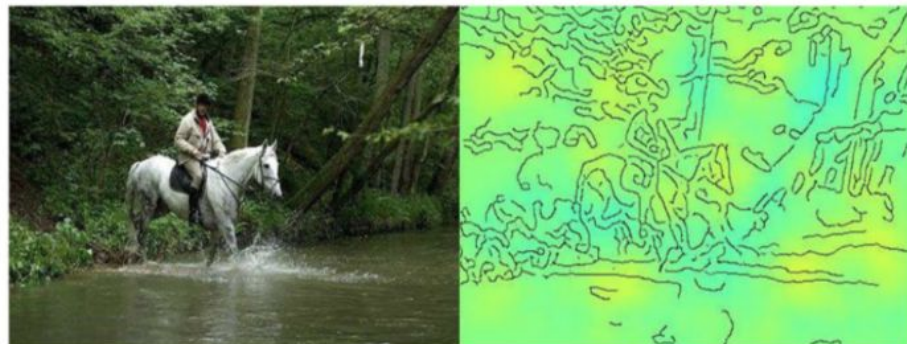
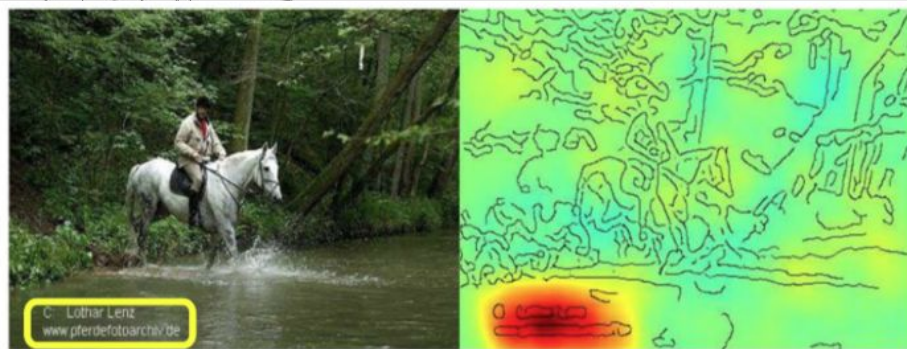
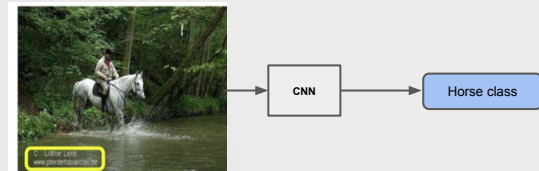
Another class

Credit [Lapuschkin et al., 2019]

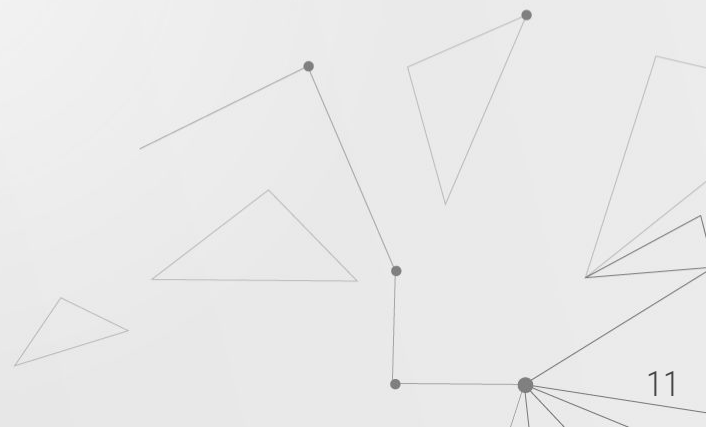
Thanks to Stefano Teso for slides

# 01 Explainability

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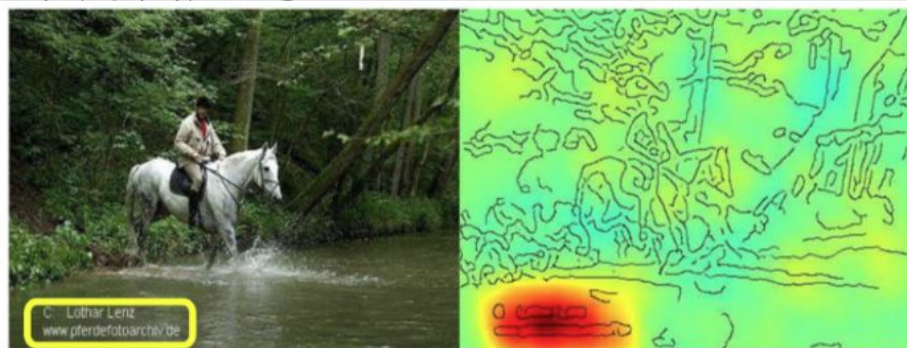
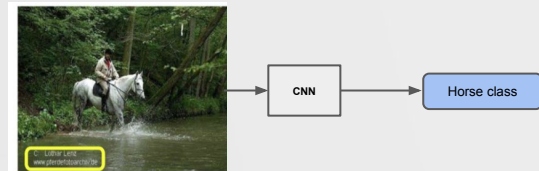


Credit [Lapuschkin et al., 2019]

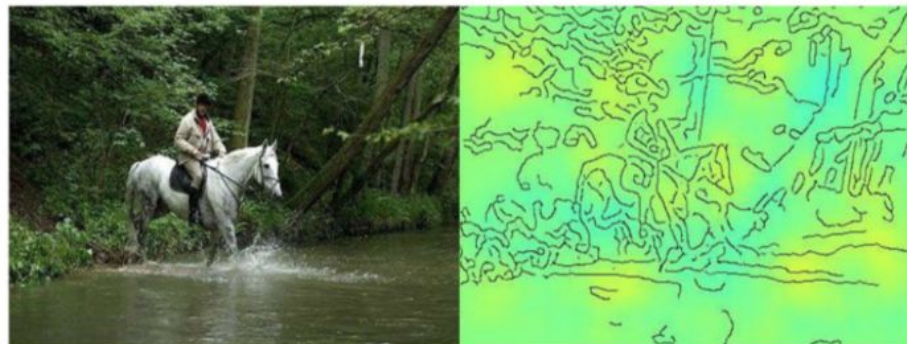


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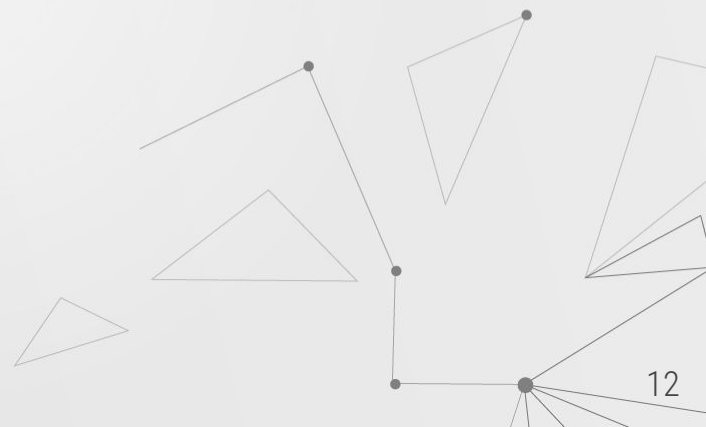
Horse-picture from Pascal VOC data set



Correlation between the presence of a watermark when an horse is present.



Credit [Lapuschkin et al., 2019]





# 01 Explainability

Explanations are studied in epistemology & philosophy of science. There are many **incompatible** but **complementary** schools of thought:

Table 1: Philosophical Theories of Explanation

	Theory	Explananda ( <i>things to be explained</i> )	Explanantia ( <i>things doing the explaining</i> )
Logical	Deductive-Nomological	Observed phenomenon or pattern of phenomena	Laws of nature, empirical observations, and deductive syllogistic pattern of reasoning
	Unification	Observed phenomenon or pattern of phenomena	Logical argument class
Causal	Transmission	Observed output of causal process	Observed or inferred trace of causal process
	Interventionist	Variables representing output of causal process	Variables representing input of causal process and invariant pattern of counterfactual dependence between variables
Functional	Pragmatic	Answers to why-questions	True propositions defined by their relevance relation to the explanandum they explain and the contrast class against which the demand for explanation is made
	Psychological	Observed phenomenon or pattern of phenomena	True propositions defined by their relation to the user's knowledge base and to the explanandum

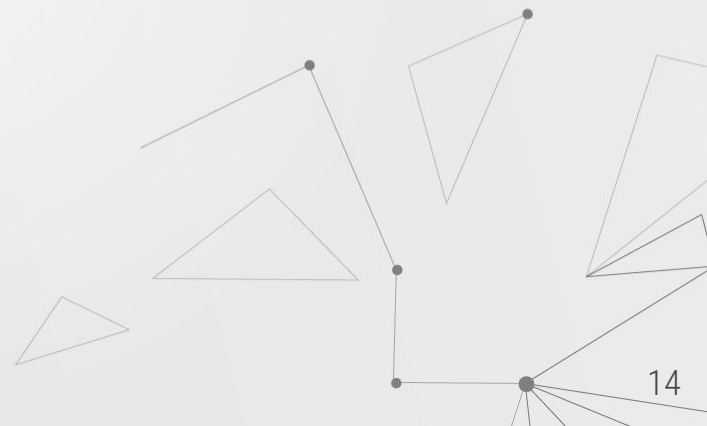


# 01 Explainability

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## Take-away:

- We need explainability!



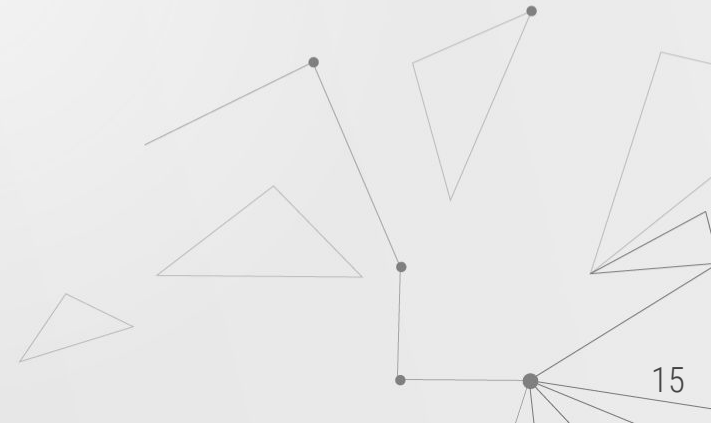


# 01 Explainability

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## Take-away:

- We need explainability!
- No unique definition of explanation, even in philosophy



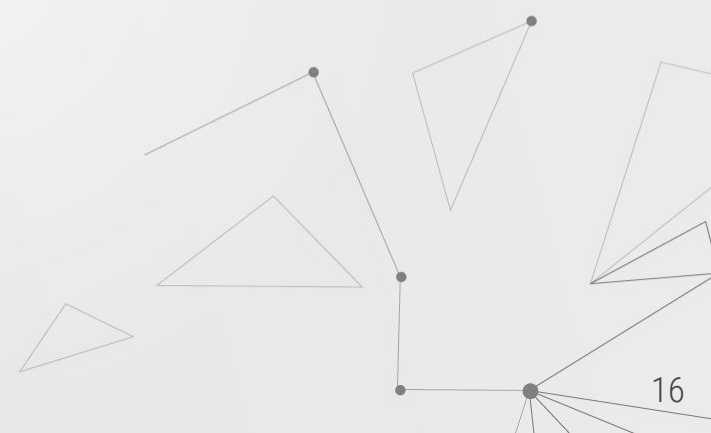


# 01 Explainability

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## Take-away:

- We need explainability!
- No unique definition of explanation, even in philosophy
- Explaining machine learning models is still an open research question



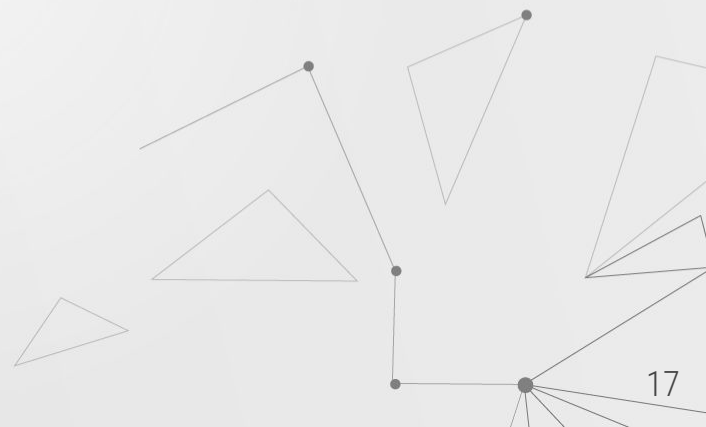




## 02 Graph Neural Networks

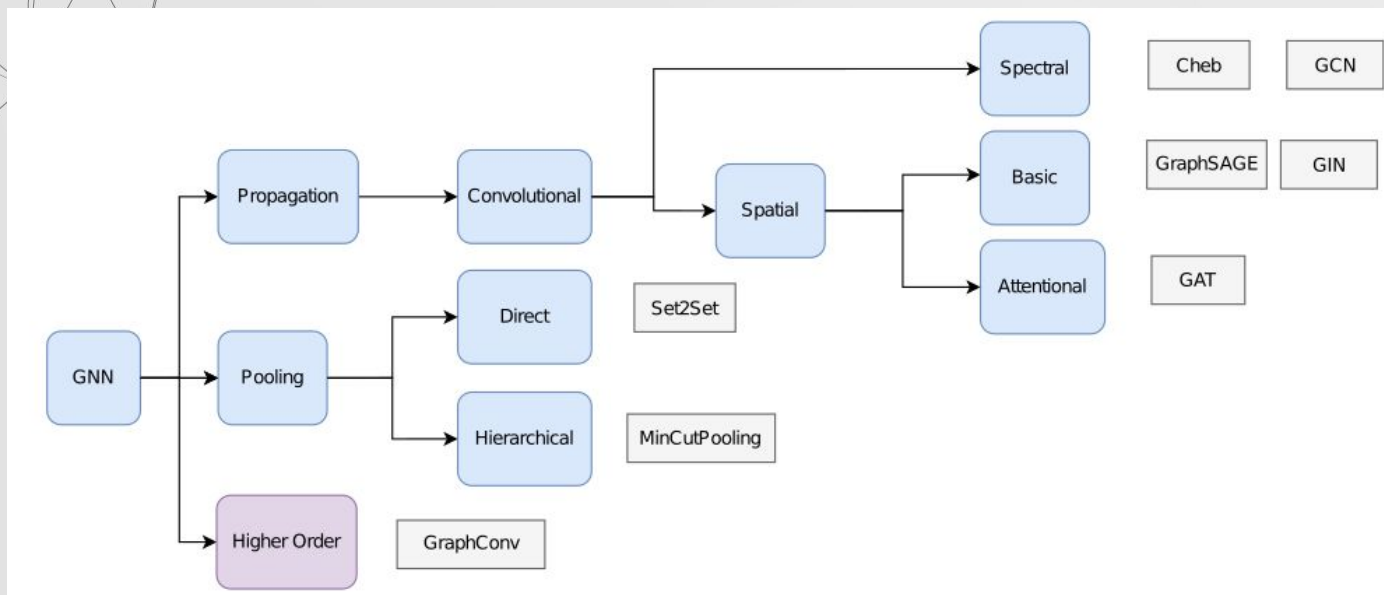
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GNN are well know to you.



# 02 Graph Neural Networks

Which network do we test?



Zhou et al. Graph neural networks: A review of methods and applications

An overview of the adopted GNN architectures structured in a taxonomy as defined by Zhou et al.

Blue boxes → Zhou et al.

Pink box → Our extension

# 02 Graph Neural Networks

Dataset	Architecture	GNN	Fully conn.	HyperParams	LR	Epochs	Train Acc	Test Acc
GRID	GCN	30-30-30	10-2	-	0.001	1500	0.994	0.998
	GRAPHSAGE	30-30-30	10-2	-	0.01	3000	X	X
	GAT	30-30-30	10-2	heads = 1	0.01	3000	X	X
	GIN	30-30	30-2	-	0.001	1000	1.0	1.0
	CHEB	30-30	30-2	-	0.001	1000	1.0	1.0
	MINCUTPOOL	32-32-32	32-2	-	0.001	700	0.92	0.93
	SET2SET	30-30-30	10-2	-	0.001	1500	0.97	0.97
	GRAPHCONV	30-30	30-2	-	0.001	500	1.0	1.0
GRID-HOUSE	GCN	60-60-60-60	60-10-2	-	0.001	7000	0.97	0.97
	GRAPHSAGE	60-60-60-60	60-10-2	-	0.01	3000	X	X
	GAT	60-60-60-60	60-10-2	heads = 3	0.01	3000	X	X
	GIN	30-30	30-2	-	0.001	1000	0.99	1.0
	CHEB	30-30-30	30-2	-	0.001	1000	1.0	0.98
	MINCUTPOOL	32-32-32	32-2	-	0.001	700	0.95	0.95
	SET2SET	60-60-60-60	60-10-2	-	0.001	1500	0.97	0.97
	GRAPHCONV	30-30	30-2	-	0.001	500	1.0	1.0
STARS	GCN	70-70-70	30-3	-	0.005	1000	0.99	1.0
	GRAPHSAGE	30-30-30	30-3	-	0.01	3000	X	X
	GAT	30-30-30	10-3	heads = 1	0.01	3000	X	X
	GIN	40-40	30-3	-	0.001	3000	0.99	1.0
	CHEB	30-30	30-3	-	0.001	1000	0.99	0.99
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Mean agg

Mean agg

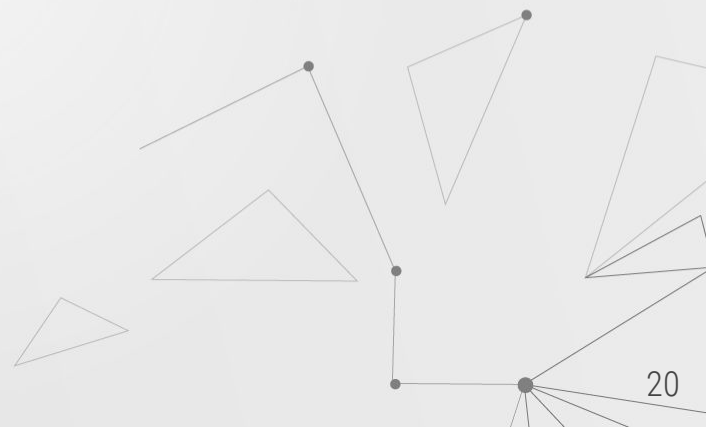
Sum agg



## 03 GNN explainers

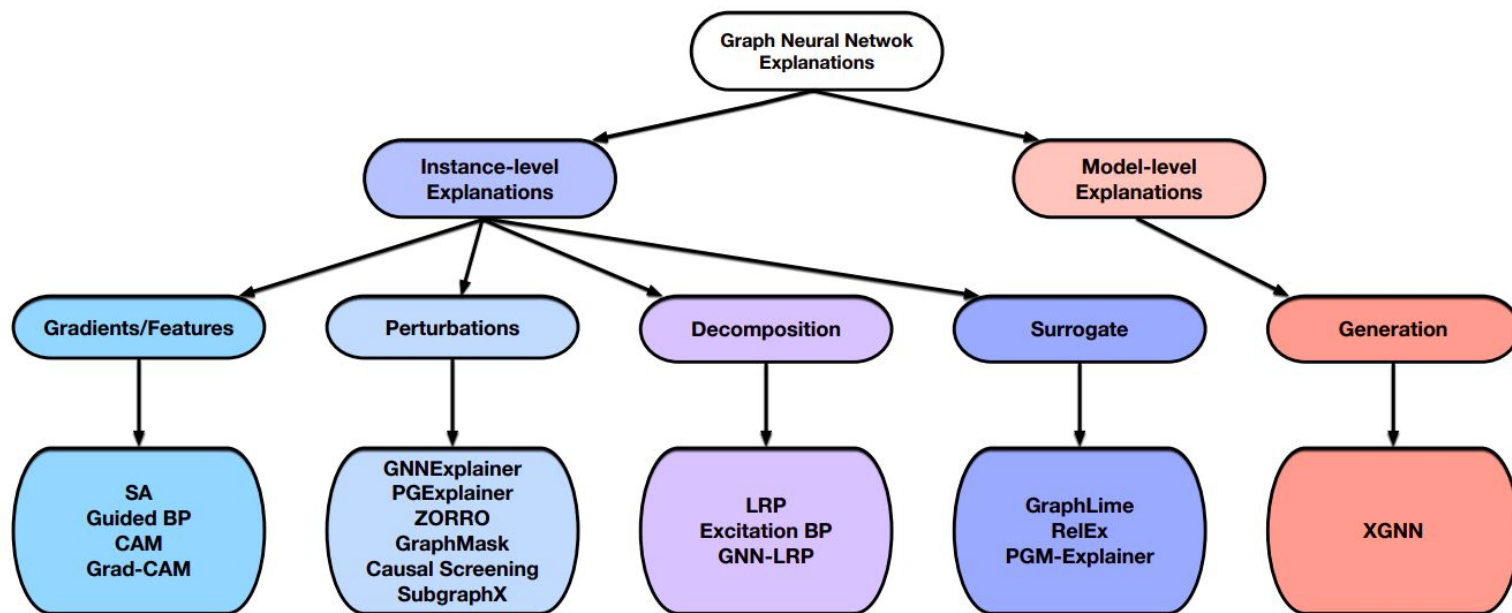
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Many GNN explainers have been proposed.



# 03 GNN explainers

Many GNN explainers have been proposed.  
We use Yuan taxonomy



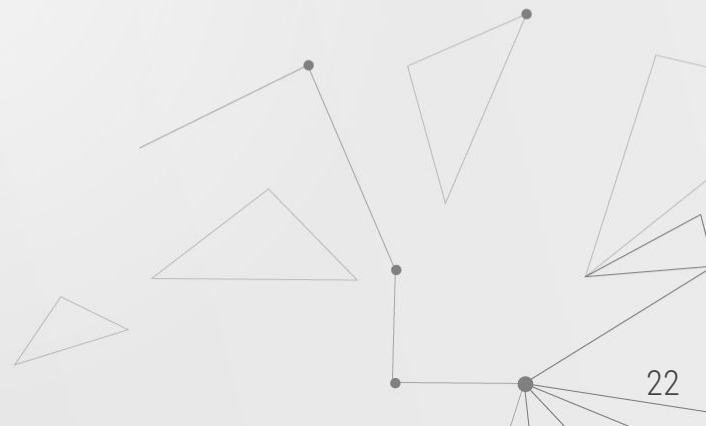
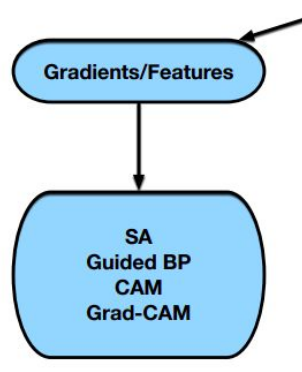
Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

# 03 GNN explainers

## Gradient/Feature based:

- They use gradients to explain the GNN.
- Widely used in image and text.
- Use the gradients as the approximations of input importance.

Yuan et al. Explainability in Graph  
Neural Networks: A Taxonomic  
Survey



# 03 GNN explainers

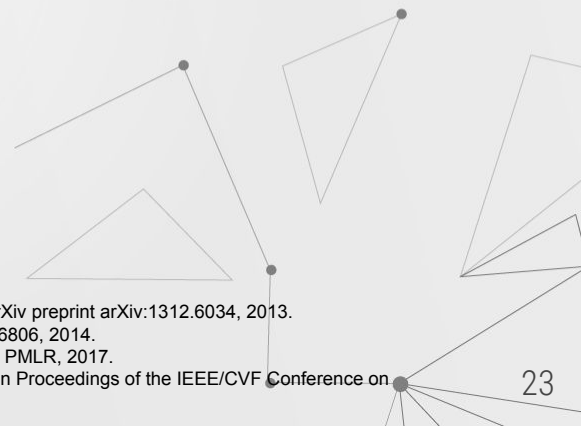
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## What we use:

- GradExplNode [1] → Node importance mask
- GuidedBP [2] → Node importance mask
- IGNode [3] → Node importance mask
- CAM [4] → Node importance mask
- GradCAM [4] → Node importance mask
- GradExplEdge [1] → Edge importance mask
- IGEEdge [3] → Edge importance mask



[1] Karen Simonyan, Andrea Vedaldi, and Andrew Zisserman. Deep inside convolutional networks: Visualising image classification models and saliency maps. arXiv preprint arXiv:1312.6034, 2013.

[2] Jost Tobias Springenberg, Alexey Dosovitskiy, Thomas Brox, and Martin Riedmiller. Striving for simplicity: The all convolutional net. arXiv preprint arXiv:1412.6806, 2014.

[3] Mukund Sundararajan, Ankur Taly, and Qiqi Yan. Axiomatic attribution for deep networks. In International conference on machine learning, pages 3319–3328. PMLR, 2017.

[4] Phillip E Pope, Soheil Kolouri, Mohammad Rostami, Charles E Martin, and Heiko Hoffmann. Explainability methods for graph convolutional neural networks. In Proceedings of the IEEE/CVF Conference on Computer Vision and Pattern Recognition, pages 10772–10781, 2019.

# 03 GNN explainers

## Perturbation based:

- Study the output variations with respect to different input perturbations
- Widely used in image and text.
- Key idea → perturb important input information should impact the prediction

Perturbations

GNNE explainer  
PGExplainer  
ZORRO  
GraphMask  
Causal Screening  
SubgraphX

Yuan et al. Explainability in Graph  
Neural Networks: A Taxonomic  
Survey



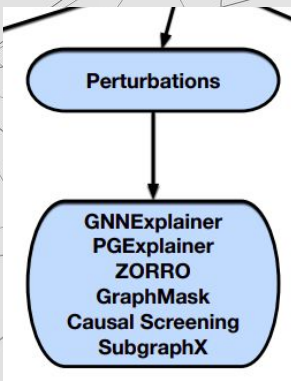
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## What we use:

- GNNexplainer [5] → Edge importance mask
- PGExplainer [6] → Edge importance mask



Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

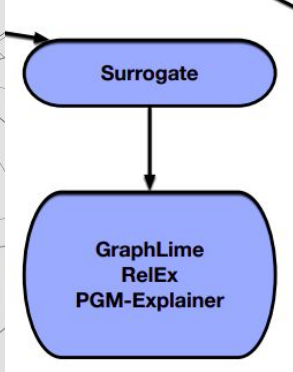
[5] Zhitao Ying, Dylan Bourgeois, Jiaxuan You, Marinka Zitnik, and Jure Leskovec. Gnnexplainer: Generating explanations for graph neural networks. Advances in neural information processing systems, 32, 2019.

[6] Dongsheng Luo, Wei Cheng, Dongkuan Xu, Wenchao Yu, Bo Zong, Haifeng Chen, and Xiang Zhang. Parameterized explainer for graph neural network. Advances in neural information processing systems, 33:19620–19631, 2020.

# 03 GNN explainers

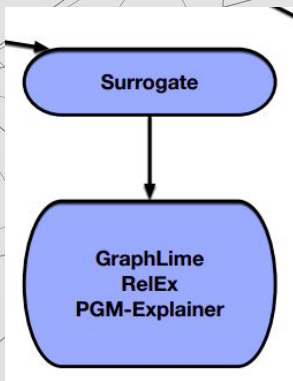
## Perturbation based:

- Use a surrogate interpretable model to approximate the prediction.



Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

# 03 GNN explainers



Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

## Perturbation based:

- Use a surrogate interpretable model to approximate the prediction.

## What we use:

- PGM-Explainer [7] → Node importance mask

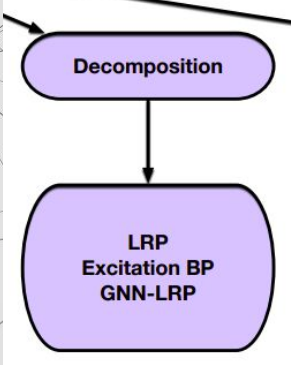
[5] Zhitao Ying, Dylan Bourgeois, Jiaxuan You, Marinka Zitnik, and Jure Leskovec. Gnnexplainer: Generating explanations for graph neural networks. Advances in neural information processing systems, 32, 2019.

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# 03 GNN explainers

## Decomposition based:

- Decompose the original model prediction into several terms.
- Study the importance of those terms wrt the input feature

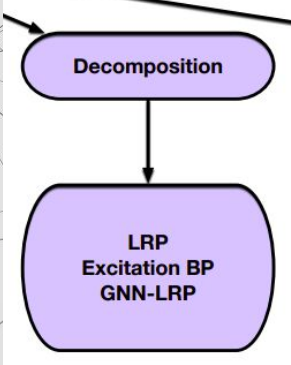


Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

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## Decomposition based:

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Yuan et al. Explainability in Graph Neural Networks: A Taxonomic Survey

## Model-level- based:

- XGNN [8]
- GLGExplainer [9]

[8] Hao Yuan, Jiliang Tang, Xia Hu, and Shuiwang Ji. Xgnn: Towards model-level explanations of graph neural networks. In Proceedings of the 26th ACM SIGKDD International Conference on Knowledge Discovery & Data Mining, pages 430–438, 2020.

[9] Steve Azzolin, Antonio Longa, Pietro Barbiero, Pietro Liò, and Andrea Passerini. Global explainability of gnns via logic combination of learned concepts, 2022

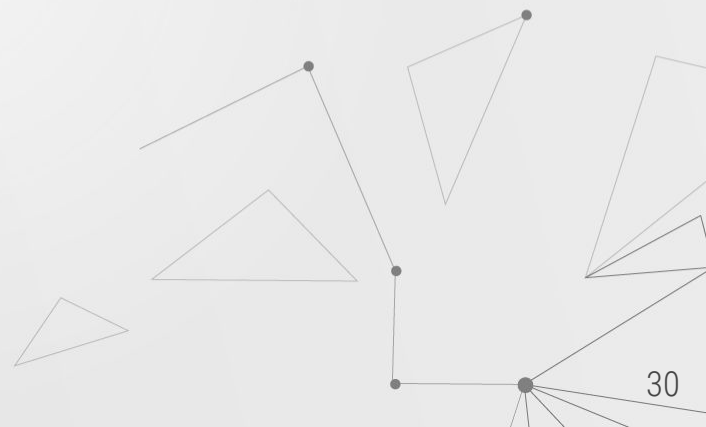


# 04 Benchmark datasets

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## Graph Classification:

- Grid
- Grid-House
- Stars
- House-Color



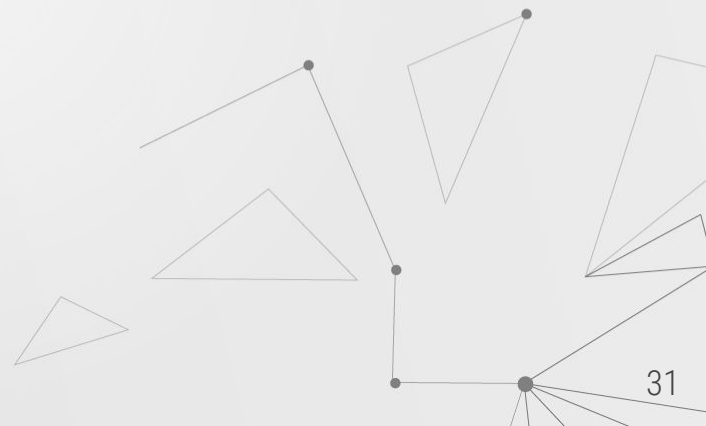


# 04 Benchmark datasets

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## Grid:

- Binary graph classification
- Classes:
  - 0  $\rightarrow$  BA random graph
  - 1  $\rightarrow$  BA random graph + 3x3 grid graph

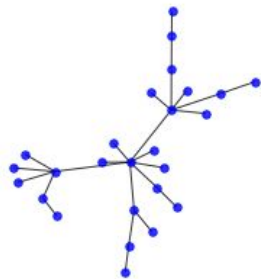


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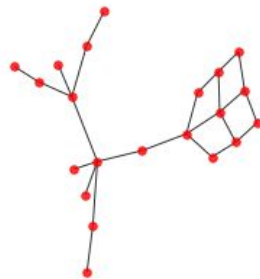
## Grid:

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Class 0



Class 1





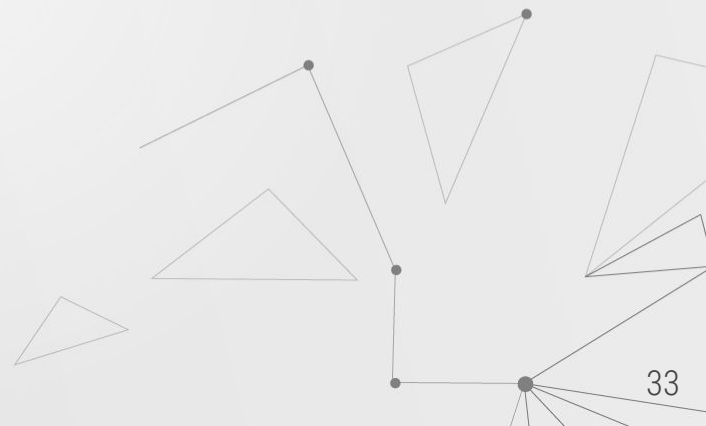


# 04 Benchmark datasets

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## Grid house:

- Binary graph classification
- Classes:
  - 0  $\rightarrow$  BA random graph + 3x3 grid graph **OR** 5 node house graph
  - 1  $\rightarrow$  BA random graph + 3x3 grid graph **AND** 5 node house graph

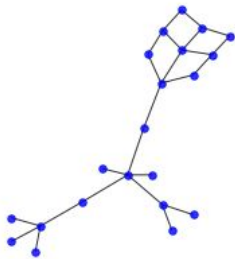


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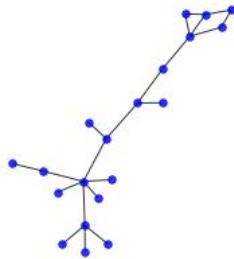
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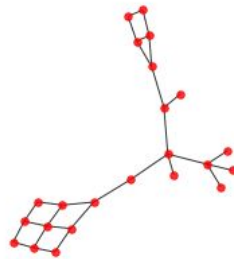
Class 0



Class 0



Class 1



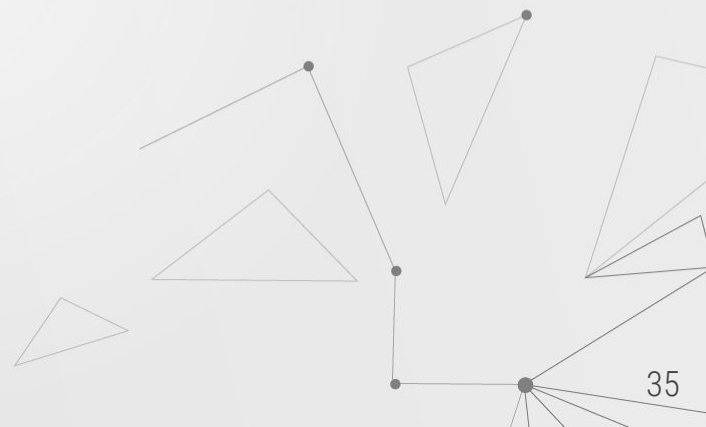


# 04 Benchmark datasets

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## Stars:

- 3 class graph classification
- Classes:
  - $0 \rightarrow$  ER random graph + 1 star
  - $1 \rightarrow$  ER random graph + 2 stars
  - $2 \rightarrow$  ER random graph + 3 stars **OR** 4 stars

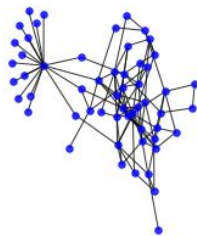


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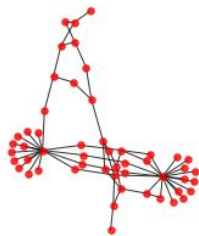
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Class 0



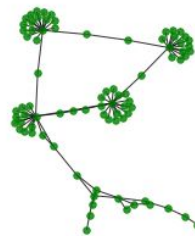
Class 1



Class 2



Class 2



# Evaluation

Plausibility

Explanation

$$P = \text{AucROC}(G_{\text{exp}}, \bar{G}_{\text{exp}}),$$

Binary GT

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Plausibility

$$P = \text{AucROC}(G_{\text{exp}}, \bar{G}_{\text{exp}}),$$

Explanation

Binary GT

Fidelity

$$F_{f1} = 2 \frac{(1 - F_{\text{suf}}) \cdot F_{\text{com}}}{(1 - F_{\text{suf}}) + F_{\text{com}}}.$$

# Evaluation

Plausibility

Explanation

$$P = \text{AucROC}(G_{\text{exp}}, \overline{G}_{\text{exp}}),$$

Binary GT

Fidelity

$$F_{f1} = 2 \frac{(1 - F_{suf}) \cdot F_{com}}{(1 - F_{suf}) + F_{com}}.$$

$$F_{suf} = \frac{1}{N_t - 1} \sum_{k=1}^{N_t - 1} (g(G) - g(G_{\text{exp}}(t_k))),$$

$$F_{com} = \frac{1}{N_t - 1} \sum_{k=1}^{N_t - 1} (g(G) - g(G \setminus G_{\text{exp}}(t_k))),$$

# So far...

- 8 GNN architectures
- 10 Explainers
- 3 Dataset (6 in the paper)

## What we can do?



# So far...

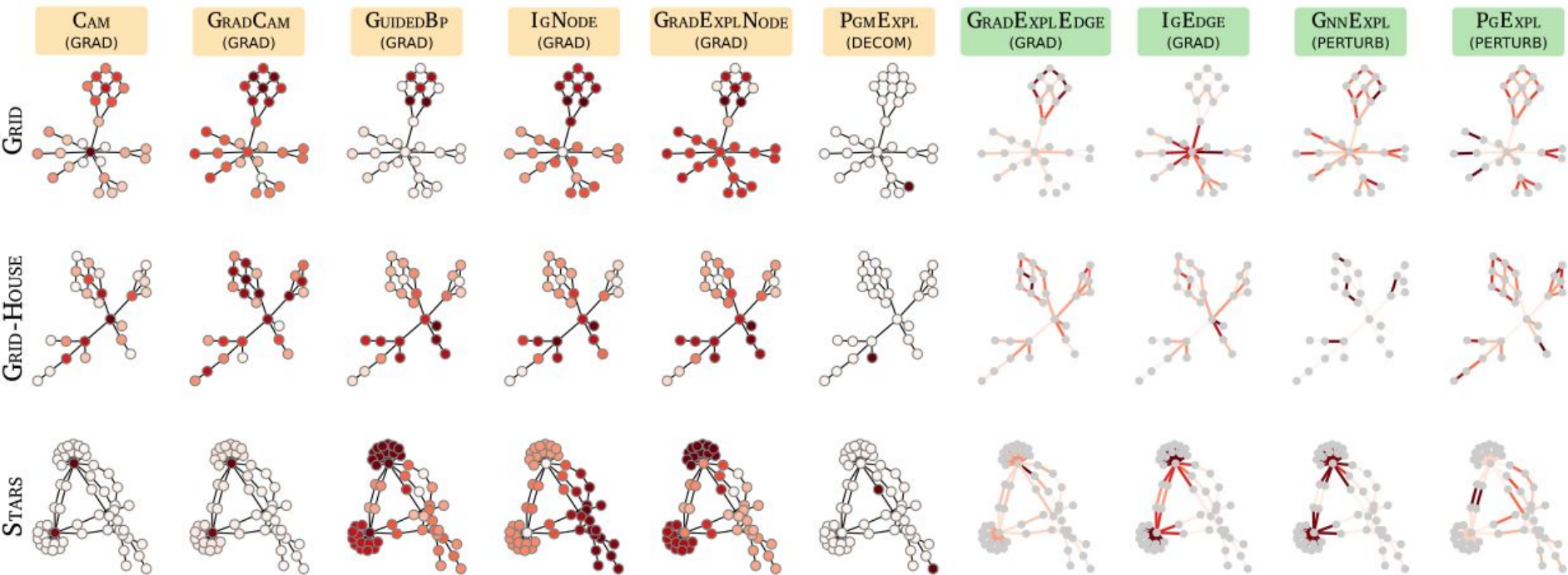
- 8 GNN architectures
- 10 Explainers
- 3 Dataset (6 in the paper)

## What we can do?

$8 \times 10 \times 6 \times (1000 \text{ graphs}) = 480\,000 \text{ (explanations)}$

Do not waste time (**and energy**)! If you need, they are available here:  
<https://github.com/AntonioLonga/GraphXAI/tree/main/Explanations>

# Look at them!





# 05 Research Questions

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- RQ1: How does the architecture affect the explanations?
- RQ2: How do explainers affect the explanations?
- RQ3: How do different types of data affect the explanations?

# 05 Research Questions

**RQ1:** How does the architecture affect the explanations?

- RQ1.1: Which is the architecture that has the best explanation?
- RQ1.2: Which is the easiest architecture to explain?
- RQ1.3: Which is the hardest architecture to explain?

	Plausibility			
	All	GRID	GRID-HOUSE	STARS
RQ1.1	<b>GRAPHCONV</b>	GRAPHCONV	CHEB	SET2SET
RQ1.2	<b>GcN</b>	CHEB	GcN	SET2SET
RQ1.3	<b>GIN</b>	GIN	GIN	MinCutPool

	Fidelity			
	All	GRID	GRID-HOUSE	STARS
RQ1.1	<b>GRAPHCONV</b>	CHEB	SET2SET	GRAPHCONV
RQ1.2	<b>GcN</b>	GcN	MinCutPool	GRAPHCONV
RQ1.3	<b>GIN</b>	GIN	GIN	MinCutPool

# 05 Research Questions

## RQ2: How do explainers affect the explanations?

- RQ2.1: Which is the explainer that explains in the best way?
- RQ2.2: Which is the explainer that explains the maximum number of architectures?
- RQ2.3: Which is the category of explainers that provides the best explanations? (Grad, Pert, Dec)
- RQ2.4: Which is the best mask type between node and edge?

Plausibility				
	All	GRID	GRID-HOUSE	STARS
RQ2.1	<b>GRADEXPLEDGE</b>	IGEDGE	PGEXPL	IGEDGE
RQ2.2	<b>GRADEXPLEDGE</b>	GRADEXPLEDGE	PGEXPL	GRADEXPLEDGE
RQ2.3	<b>Pert</b>	Pert	Pert	Grad
RQ2.4	<b>Edge</b>	Edge	Edge	Edge

Fidelity				
	All	GRID	GRID-HOUSE	STARS
RQ2.1	<b>IGEDGE</b>	PGEXPL	IGEDGE	GRADEXPLEDGE
RQ2.2	<b>IGEDGE</b>	IGEDGE	IGEDGE	GNNEXPL
RQ2.3	<b>Pert</b>	Pert	Pert	Pert
RQ2.4	<b>Edge</b>	Edge	Edge	Edge



# 05 Research Questions

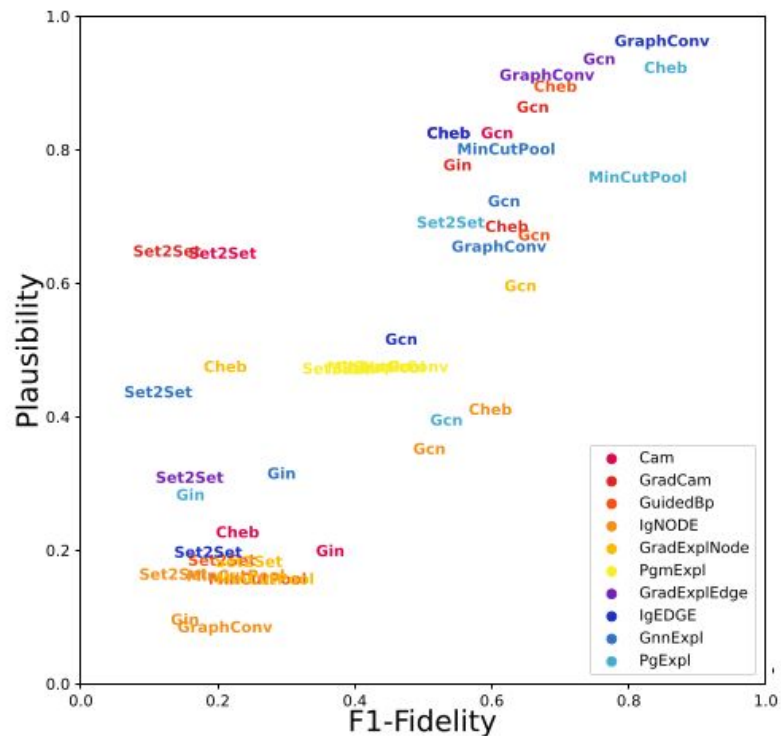
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**RQ3:** How do different types of data affect the explanations?

# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

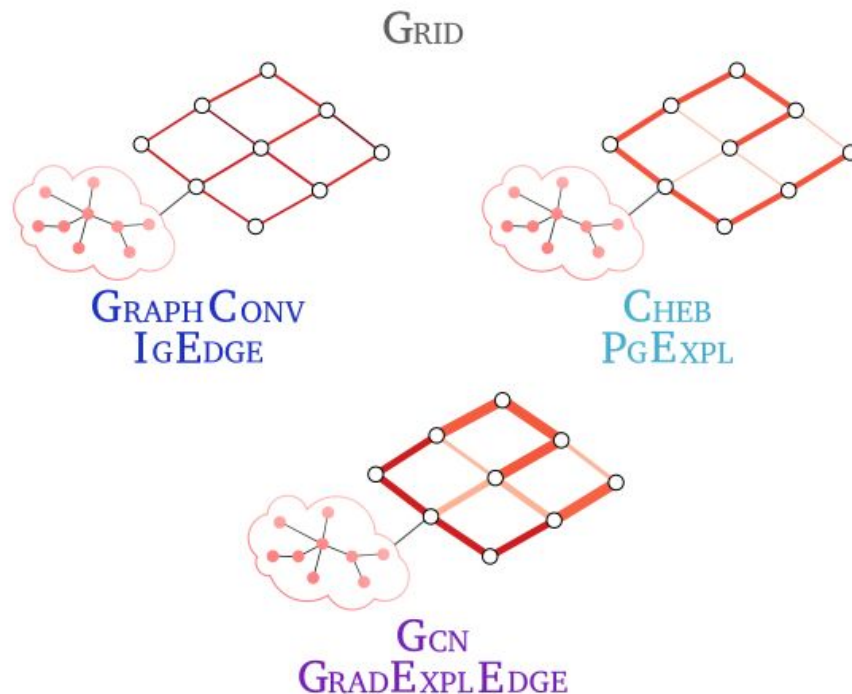
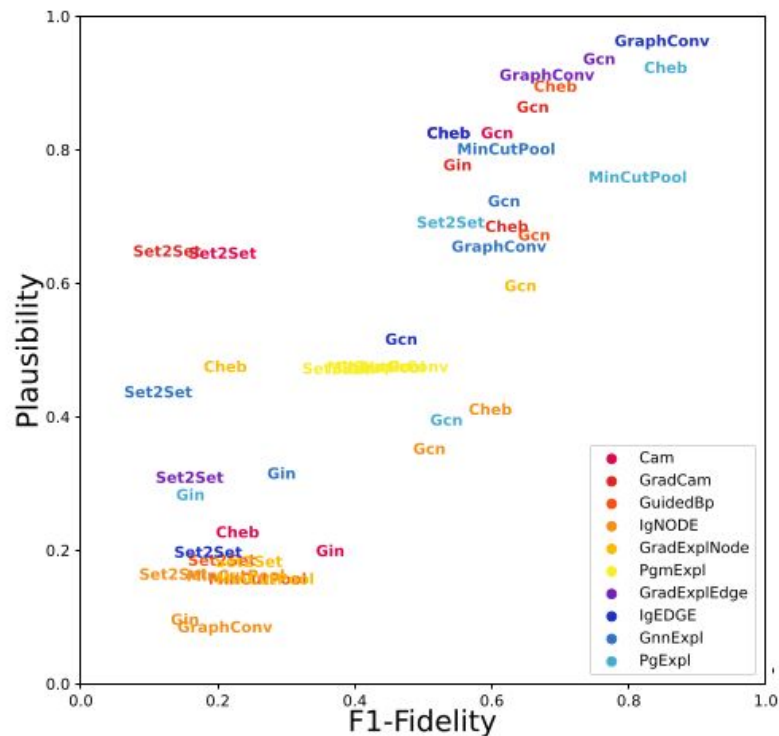
**GRID**



# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

## GRID

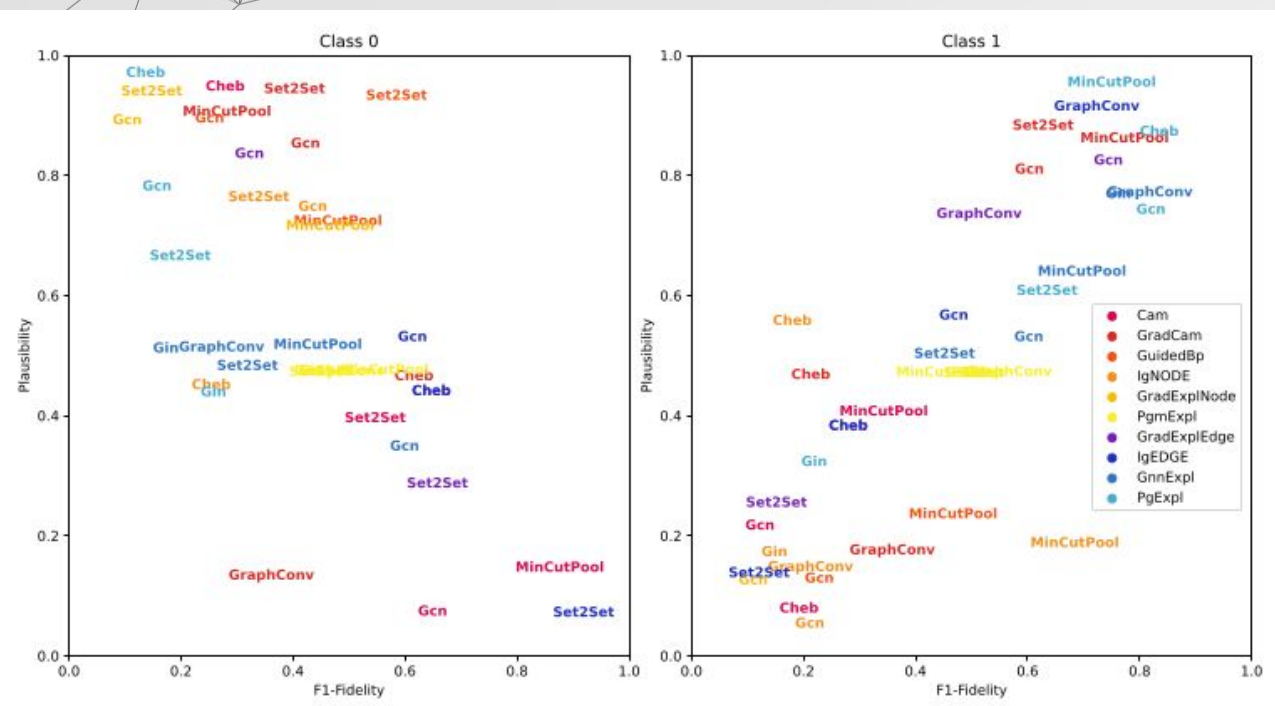




# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

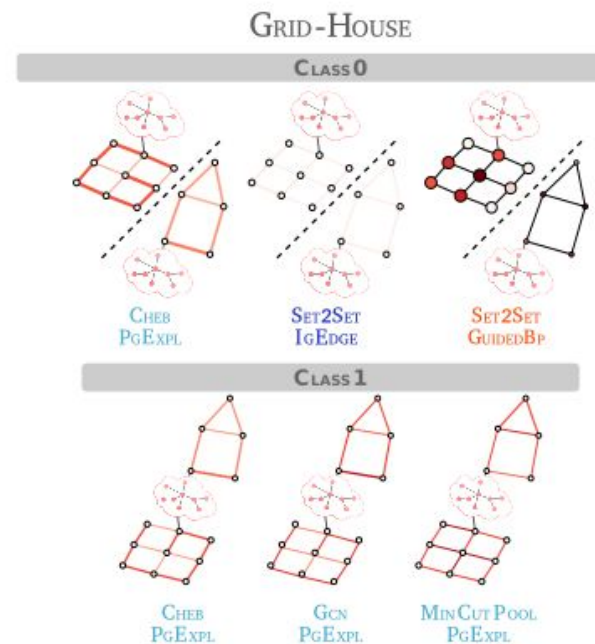
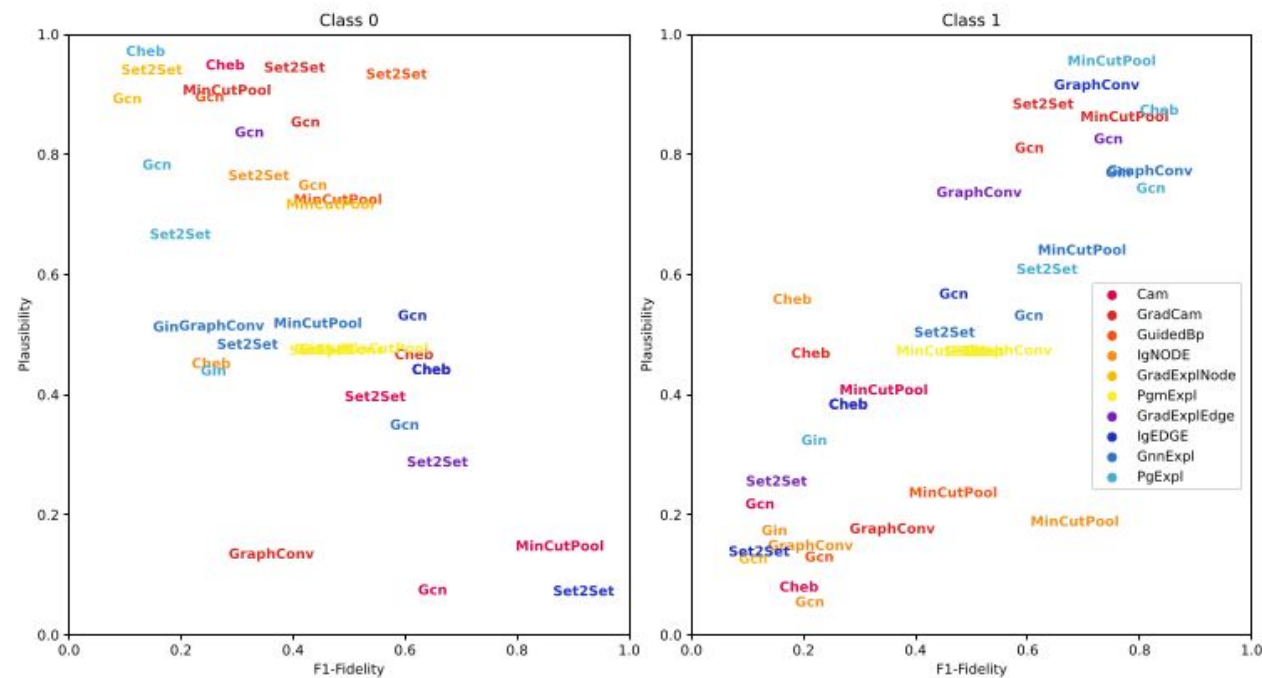
## GRID HOUSE



# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

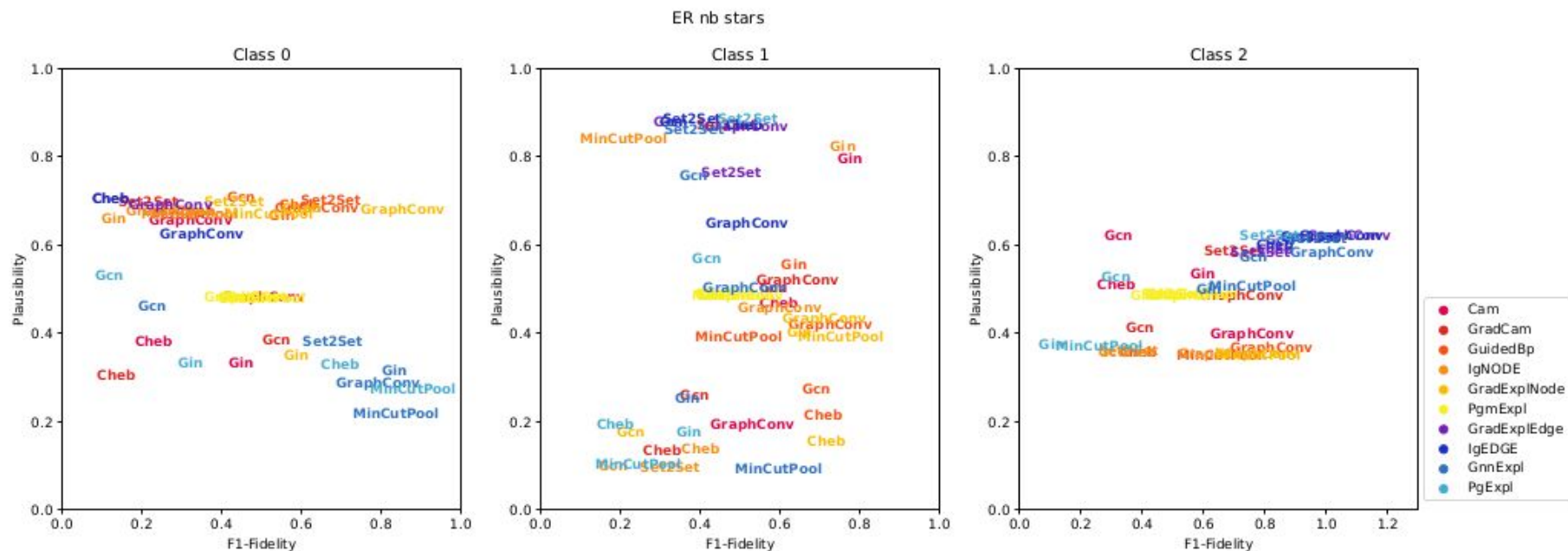
## GRID HOUSE



# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

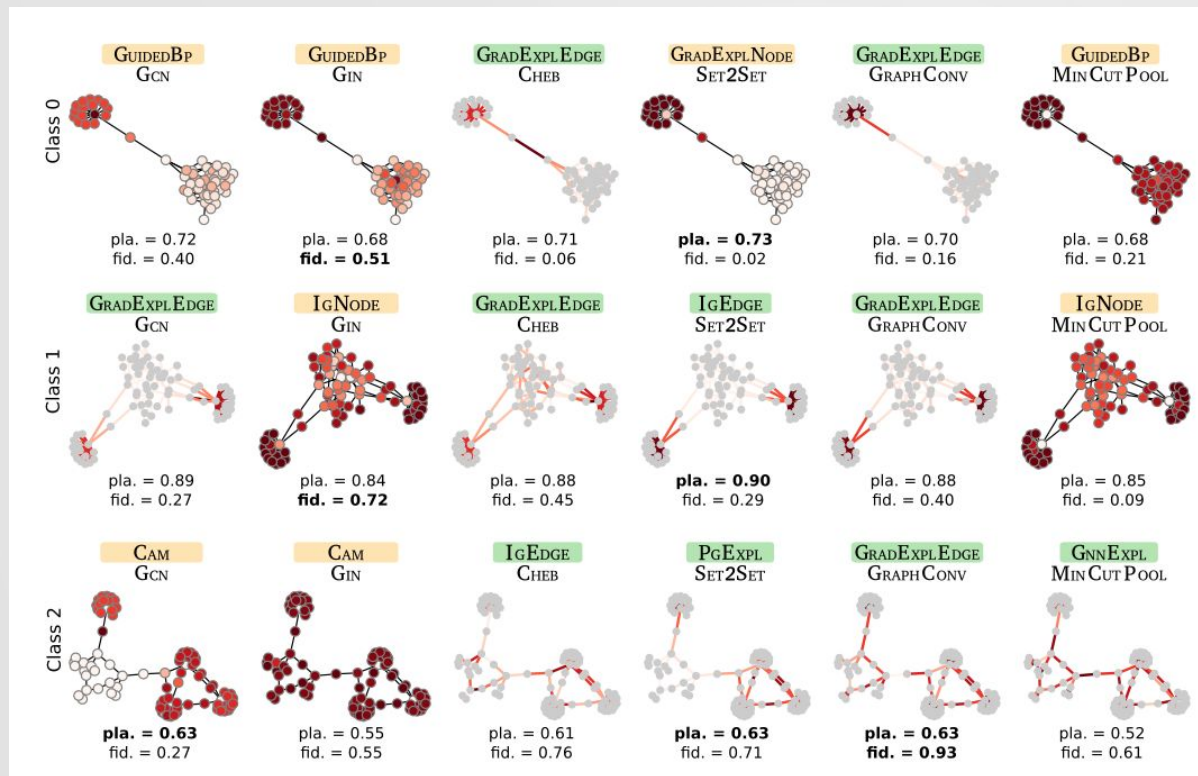
## STARS



# 05 Research Questions

**RQ3:** How do different types of data affect the explanations?

## STARS





## 06 Conclusion & future directions

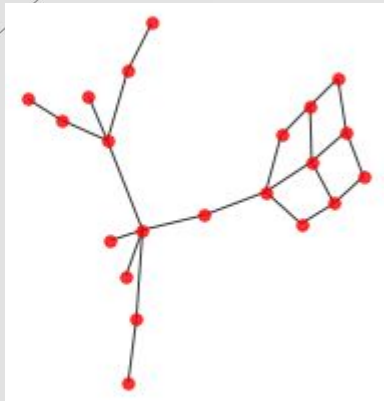
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- 1) Human bias when defining Ground Truth.
  - a) In GRID network do we need the entire grid?

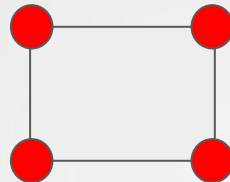


# 06 Conclusion & future directions

- 1) Human bias when defining Ground Truth.
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A square is enough

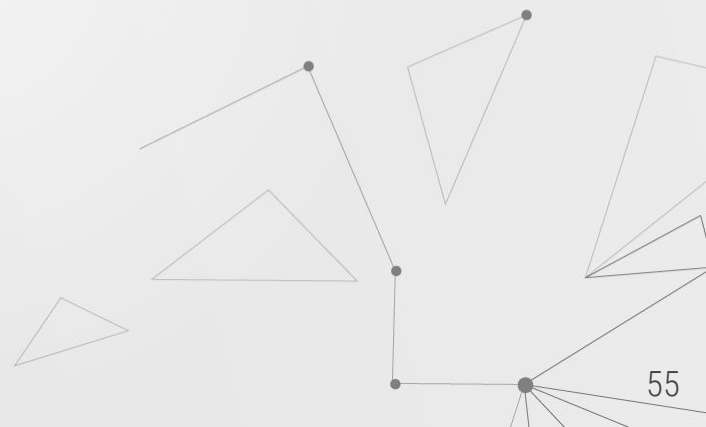




## 06 Conclusion & future directions

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- 1) Human bias when defining Ground Truth.
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## 06 Conclusion & future directions

---

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  - a) NOPE

**Graph Classification**

**STARS**

**Node Classification**







## 06 Conclusion & future directions

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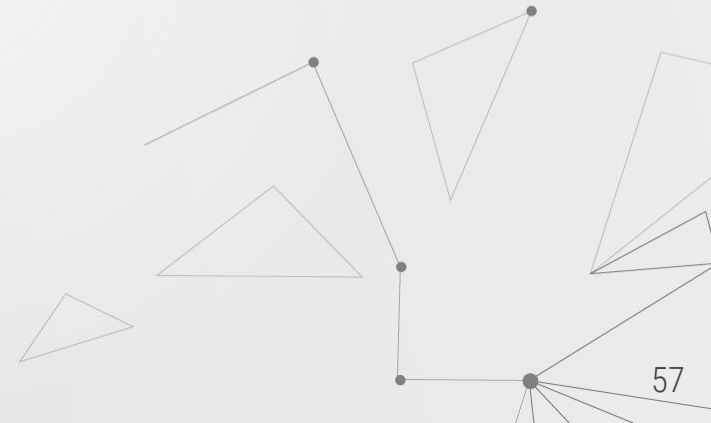
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### Graph Classification

#### STARS

- 1) Identify stars
- 2) Count them
- 3) Classify according to the frequency of stars

### Node Classification



# 06 Conclusion & future directions

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## Graph Classification

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Node embedding → **SUM** → Graph embedding

## Node Classification

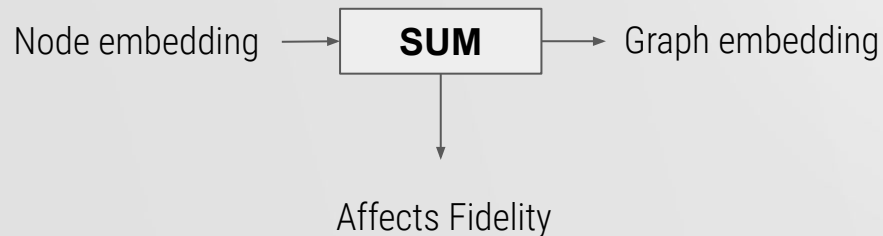
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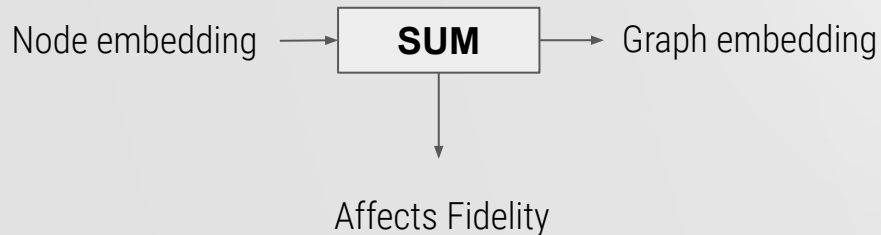
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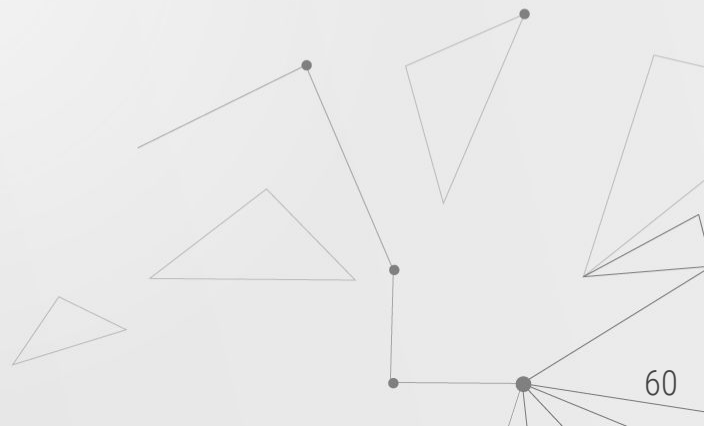
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## Node Classification

- 1) Comprehensiveness → difficult to define



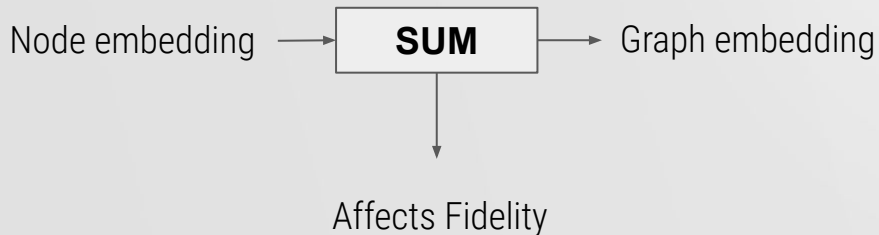
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### Only sufficiency

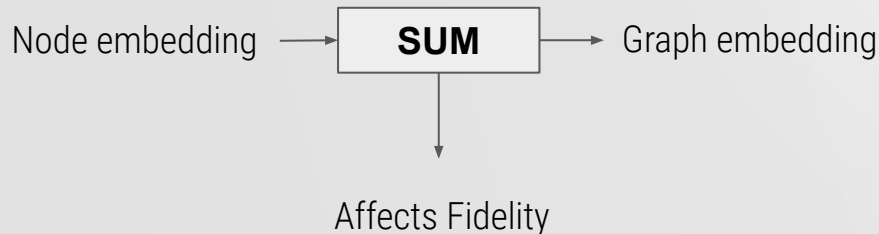
# 06 Conclusion & future directions

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## Graph Classification

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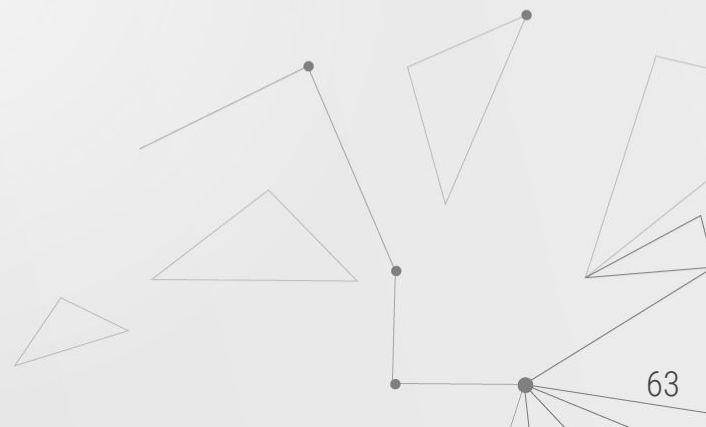
The entire graph has the perfect score!!!




## 06 Conclusion & future directions

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- 1) Human bias when defining Ground Truth.
  - a) In GRID network do we need the entire grid?
- 2) We could use only the fidelity...
  - a) NOPE
- 3) Overall it seems that:
  - a) Node Classification → Gradient based.
  - b) Graph Classification → Edge mask based on Gradient or Perturbation.





Thanks!  
Do you have any questions?

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